

Probability

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Probability

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Comprehensive study notes for

Probability

by

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(Math King of Katargam). Master every concept with clear explanations, solved examples, and practice problems.

Key Concepts

Introduction

Probability

measures the likelihood of an event occurring. It ranges from 0 (impossible) to 1 (certain).

Experiment:

A process with well-defined outcomes.

Random experiment:

Cannot predict the outcome with certainty.

Trial and Event

A

trial

is a single performance of an experiment. An

event

is a specific outcome or set of outcomes.

Empirical probability:

Based on actual experiments and observations.

Empirical Probability Formula

$P(E) = (\text{Number of times event } E \text{ occurs}) / (\text{Total number of trials})$. For example, if a coin is tossed 100 times and heads appears 52 times, $P(\text{heads}) = 52/100 = 0.52$.

Key Properties

$0 \leq P(E) \leq 1$. $P(E) + P(\text{not } E) = 1$. If $P(E) = 0$, the event is impossible. If $P(E) = 1$, the event is certain. As the number of trials increases, the empirical probability approaches the theoretical probability.

Coin Toss

For a fair coin: $P(\text{Heads}) = 1/2$, $P(\text{Tails}) = 1/2$. For two coins: $P(\text{both heads}) = 1/4$, $P(\text{one head one tail}) = 1/2$, $P(\text{both tails}) = 1/4$.

Dice Roll

For a fair die: $P(\text{getting any number } 1-6) = 1/6$. $P(\text{even number}) = 3/6 = 1/2$. $P(\text{number} > 4) = 2/6 = 1/3$.

Cards

A standard deck has 52 cards: 4 suits (hearts, diamonds, clubs, spades), 13 cards each. Hearts & diamonds are red;

clubs & spades are black.

Face cards:

Jack, Queen, King (12 total).

Important Formulas

Empirical Probability

$$P(E) = (\text{Favorable outcomes})/(\text{Total trials})$$

Complement

$$P(\text{not } E) = 1 - P(E)$$

Coin Toss

$$P(H) = P(T) = 1/2$$

Single Die

$$P(\text{any number}) = 1/6$$

Cards (total)

52 cards, 4 suits, 13 per suit

Solved Examples

Example 1:

A coin is tossed 200 times and heads appear 108 times. Find $P(\text{heads})$ and $P(\text{tails})$.

Solution:

$$P(\text{heads}) = 108/200 = 0.54. P(\text{tails}) = (200-108)/200 = 92/200 = 0.46$$

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Example 2:

A die is rolled 300 times and 5 appears 48 times. Find $P(\text{getting } 5)$.

Solution:

$$P(5) = 48/300 = 0.16$$

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Example 3:

From a deck of 52 cards, what is the probability of drawing a heart?

Solution:

$$\text{There are 13 hearts. } P(\text{heart}) = 13/52 = 1/4$$

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Practice Questions

A coin is tossed 150 times and heads come up 78 times. Find $P(\text{heads})$ and $P(\text{tails})$.

A die is rolled 250 times. The number 6 appears 42 times. Find $P(6)$.

What is the probability of getting a sum of 7 when two dice are rolled?

A bag contains 5 red and 3 blue balls. Find $P(\text{red})$ and $P(\text{blue})$.

From a deck of 52 cards, find the probability of drawing a king or a queen.

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