

# Heron's Formula

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Comprehensive study notes for

Heron's Formula

by

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(Math King of Katargam). Master every concept with clear explanations, solved examples, and practice problems.

Key Concepts

Area of a Triangle

For a triangle with sides  $a$ ,  $b$ ,  $c$ , Heron's formula gives the area without needing the height.

Semi-perimeter:

$$s = (a + b + c)/2.$$

Heron's Formula

Area =  $\sqrt{s(s-a)(s-b)(s-c)}$  where  $s$  is the semi-perimeter. This formula works for ALL types of triangles - scalene, isosceles, equilateral.

Area of Equilateral Triangle

For an equilateral triangle with side  $a$ :  $s = 3a/2$ . Using Heron's formula: Area =  $\frac{\sqrt{3}}{4} \times a^2$ .

Application to Quadrilaterals

To find the area of a quadrilateral using Heron's formula, divide it into two triangles by drawing a diagonal, find the area of each, and add them.

Important Formulas

Semi-perimeter

$$s = (a + b + c)/2$$

Heron's Formula

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$

Equilateral Triangle

$$\text{Area} = \frac{\sqrt{3}}{4}a^2$$

Isosceles Triangle

$$\text{Area} = \frac{b}{4}\sqrt{4a^2 - b^2} \text{ where } a = \text{equal sides, } b = \text{base}$$

Solved Examples

Example 1:

Find the area of a triangle with sides 3 cm, 4 cm, 5 cm.

Solution:

$$s = (3+4+5)/2 = 6. \text{ Area} = \sqrt{6(6-3)(6-4)(6-5)} = \sqrt{6 \times 3 \times 2 \times 1} = \sqrt{36} =$$

$$6 \text{ cm}^2$$

. This is a 3-4-5 right triangle.

Example 2:

Find the area of an equilateral triangle with side 6 cm.

Solution:

Using direct formula:  $\text{Area} = \left(\frac{\sqrt{3}}{4}\right) \times 6^2 = \left(\frac{\sqrt{3}}{4}\right) \times 36 = 9\sqrt{3} = 15.59 \text{ cm}^2$

Example 3:

A triangular park has sides 120 m, 80 m, and 80 m. Find its area.

Solution:

$s = (120+80+80)/2 = 140$ .  $\text{Area} = \sqrt{[140(140-120)(140-80)(140-80)]} = \sqrt{(140 \times 20 \times 60 \times 60)} = \sqrt{(10080000)} = 3175 \text{ m}^2$

Practice Questions

Find the area of a triangle with sides 7 cm, 8 cm, 9 cm.

The sides of a triangle are in ratio 12:17:25 and its perimeter is 540 cm. Find its area.

Find the area of an equilateral triangle with perimeter 60 cm.

A rhombus has perimeter 40 cm and one diagonal 12 cm. Find its area.

The base of an isosceles triangle is 12 cm and perimeter is 32 cm. Find its area.

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